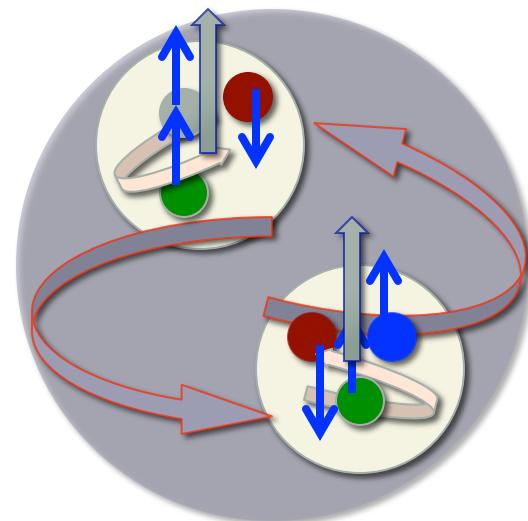


FLAVOR DEPENDENCE DETERMINATION OF TRANSVERSITY GPDS AND BSM INTERACTIONS

BNL WORKSHOP ON GPDS FOR EIC
JUNE 4TH, 2018

Simonetta Liuti
University of Virginia

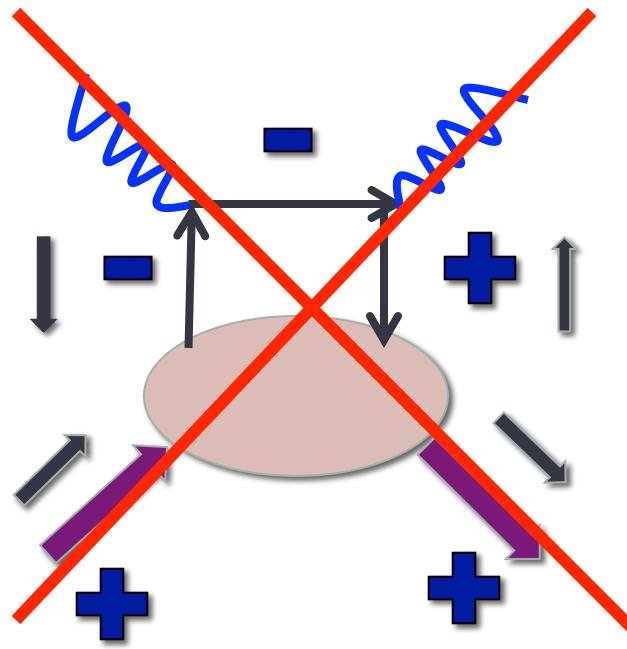


Outline

1. Introduction
2. Chiral Odd GPDs
3. Extraction from experiment: role of EIC
4. Impact on BSM searches
5. Conclusions and Outlook

1. INTRODUCTION

In a nutshell



- ✓ The **tensor charge** is not a fundamental property of strongly interacting matter within the Standard Model
- ✓ Chiral Odd constructs appear because of the **composite** structure of hadrons
- ✓ To detect chiral odd distributions we need another **distinct** hadronic blob

In 2009 we proposed

PHYSICAL REVIEW D
covering particles, fields, gravitation, and cosmology

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Nucleon tensor charge from exclusive π^0 electroproduction

Saeed Ahmad, Gary R. Goldstein, and Simonetta Liuti

Phys. Rev. D **79**, 054014 – Published 25 March 2009

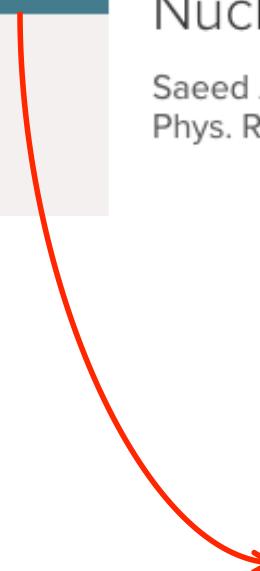
PHYSICAL REVIEW D
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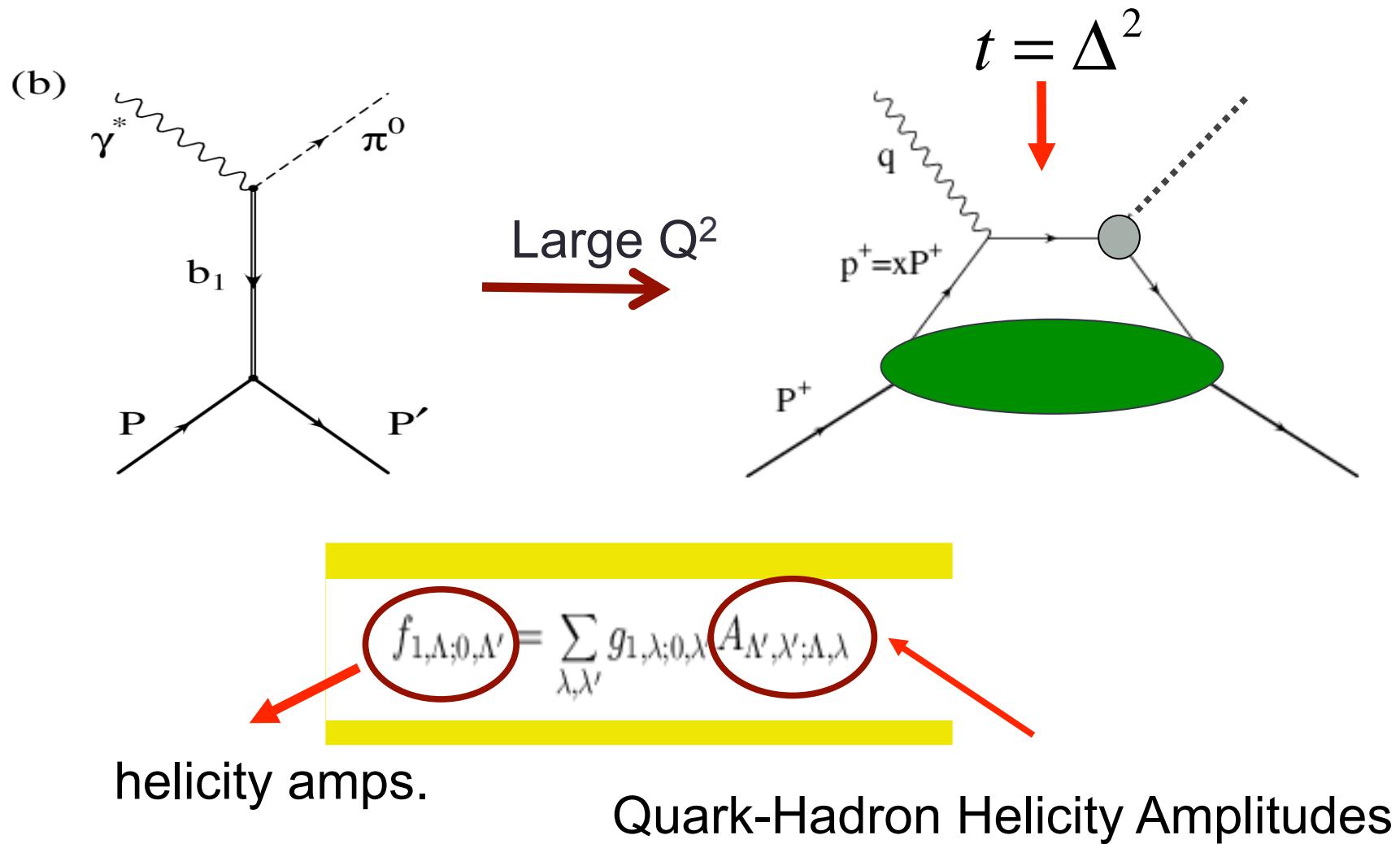
Flexible parametrization of generalized parton distributions: The chiral-odd sector

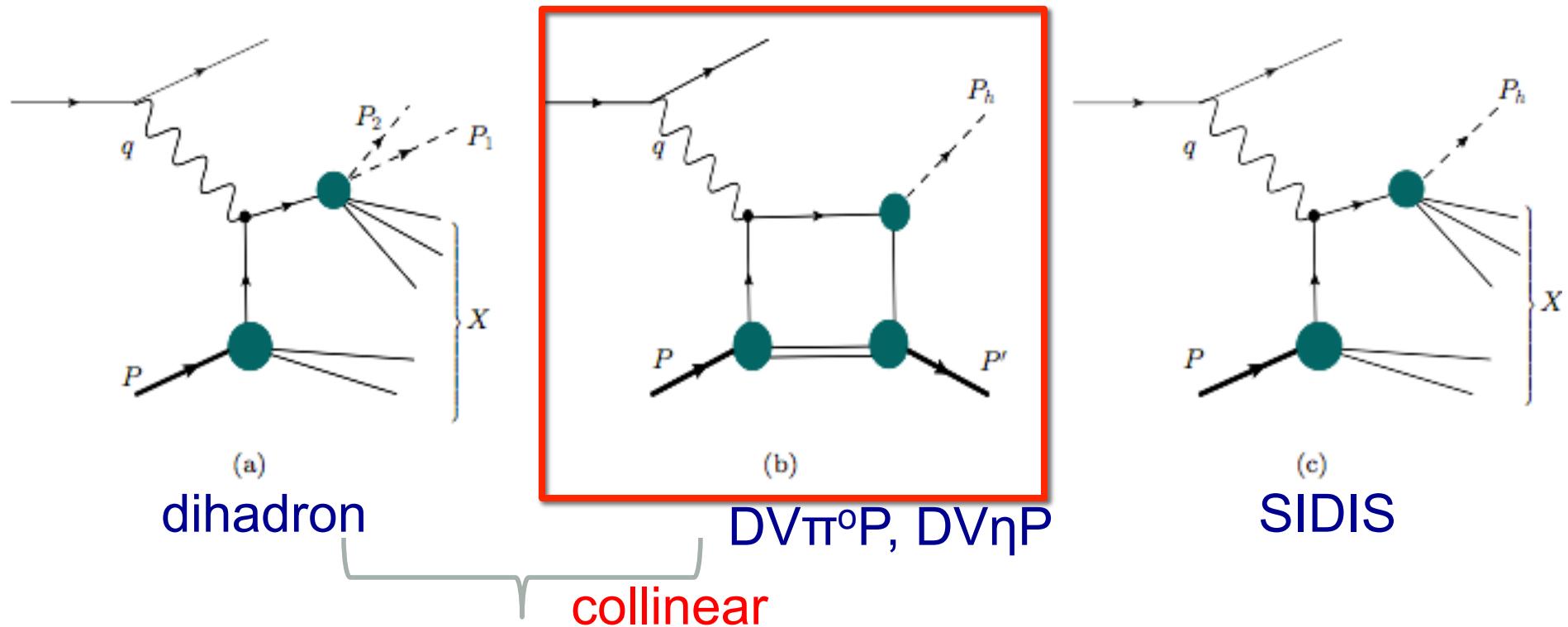
Gary R. Goldstein, J. Osvaldo Gonzalez Hernandez, and Simonetta Liuti

Phys. Rev. D **91**, 114013 – Published 8 June 2015

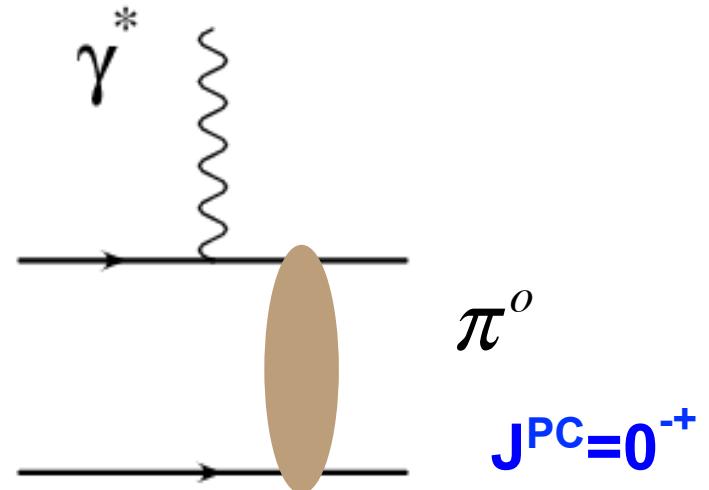
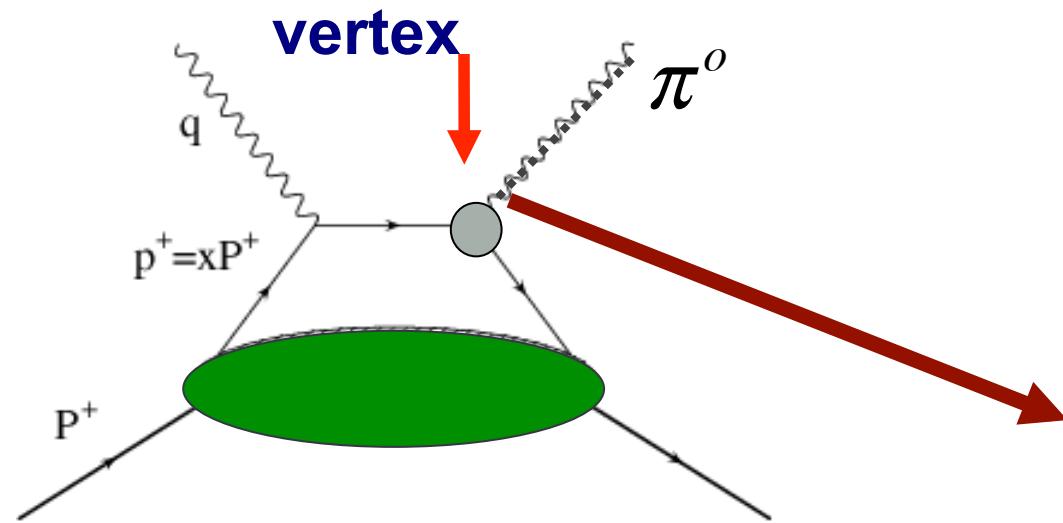


Dual Representation



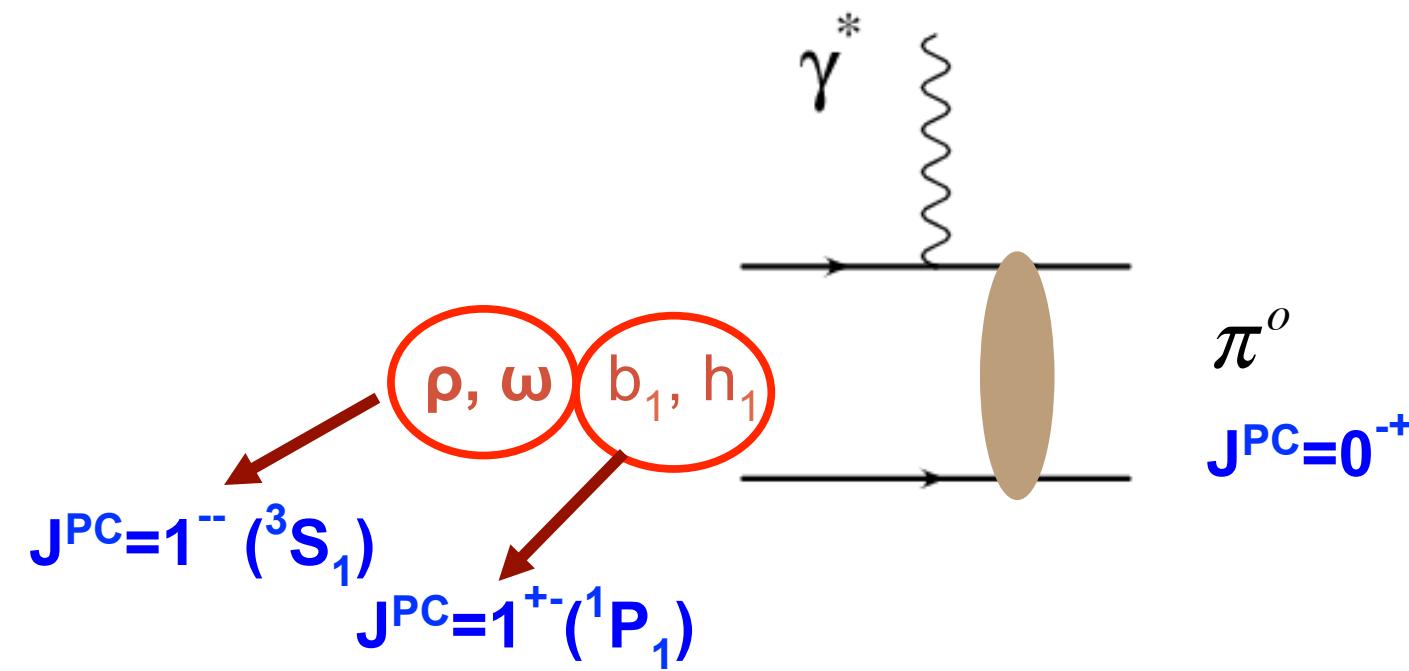


Issue: Q^2 dependence



Goloskokov and Kroll: γ_5 coupling is
of twist 3

Our model: pseudoscalar-meson transition form factor



mesons quark content: $\frac{1}{\sqrt{2}} (u\bar{u} \pm d\bar{d})$

ρ, ω (vector) and b_1, h_1 (axial-vector) exchanges

- $J^{PC}=1^{--}$ \rightarrow from ρ, ω ($S=1 L=0$) to π^o ($S=0 L=0$) $\Delta L = 0$ no change in OAM
- $J^{PC}=1^{+-}$ \rightarrow from b_1, h_1 ($S=0 L=1$) to π^o ($S=0 L=0$) $\Delta L = 1$ change 1 unit of OAM

$$F_{\gamma^* V \pi^o} = \int dx_1 dy_1 \int d^2 b \psi_V(y_1, b) C K_o(\sqrt{x_1(1-x_1)Q^2} b) \psi_{\pi^o}(x_1, b) \exp(-S)$$

$$F_{\gamma^* A \pi^o} = \int dx_1 dy_1 \int d^2 b \psi_A^{(1)}(y_1, b) C K_o(\sqrt{x_1(1-x_1)Q^2} b) \psi_{\pi^o}(x_1, b) \exp(-S)$$

Because of OAM axial vector transition involves Bessel J_1

$$\psi_A^{(1)}(y_1, b) = \int d^2 k_T J_1(y_1 b) \psi(y_1, k_T),$$

This yields configurations of larger “radius” in b space (suppressed with Q^2)

Rewrite helicity amps. expressions using new GFFs

$$f_1 = f_4 = \frac{g_2}{C_q} F_V(Q^2) \frac{\sqrt{t_0 - t}}{2M} \left[\tilde{\mathcal{H}}_T + \frac{1 - \xi}{2} \mathcal{E}_T + \frac{1 - \xi}{2} \tilde{\mathcal{E}}_T \right]$$

$$f_2 = \frac{g_2}{C_q} [F_V(Q^2) + F_A(Q^2)] \sqrt{1 - \xi^2} \left[\mathcal{H}_T + \frac{t_0 - t}{4M^2} \tilde{\mathcal{H}}_T - \frac{\xi^2}{1 - \xi^2} \mathcal{E}_T + \frac{\xi}{1 - \xi^2} \tilde{\mathcal{E}}_T \right]$$

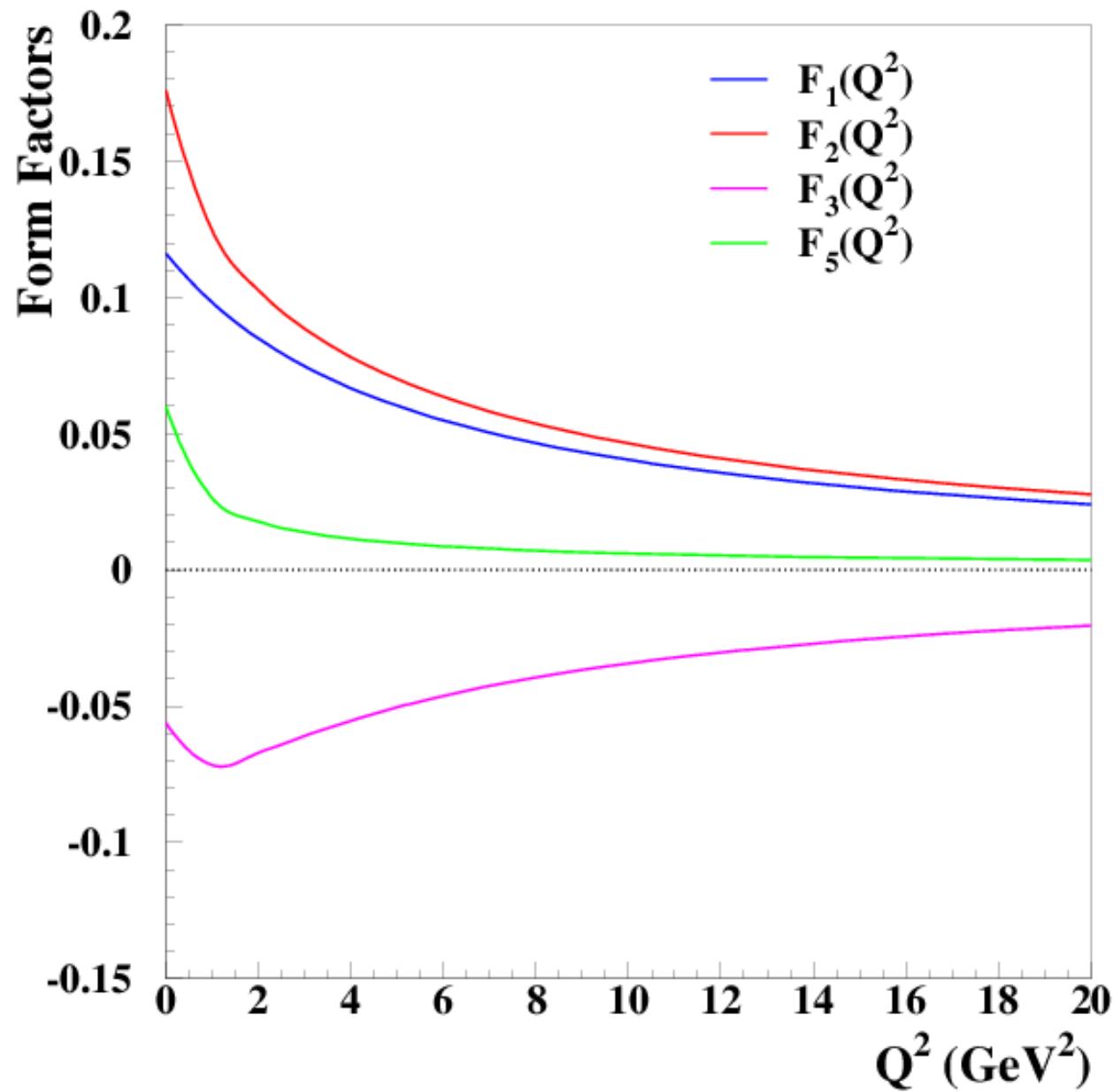
$$f_3 = \frac{g_2}{C_q} [F_V(Q^2) - F_A(Q^2)] \sqrt{1 - \xi^2} \frac{t_0 - t}{4M^2} \tilde{\mathcal{H}}_T$$

$$f_5 = \frac{g_5}{C_q} F_A(Q^2) \sqrt{1 - \xi^2} \left[\mathcal{H}_T + \frac{t_0 - t}{4M^2} \tilde{\mathcal{H}}_T - \frac{\xi^2}{1 - \xi^2} \mathcal{E}_T + \frac{\xi}{1 - \xi^2} \tilde{\mathcal{E}}_T \right],$$

elementary subprocess

Q^2 dependent pion vertex

GFFs



Does QCD factorization hold and how can we test it?

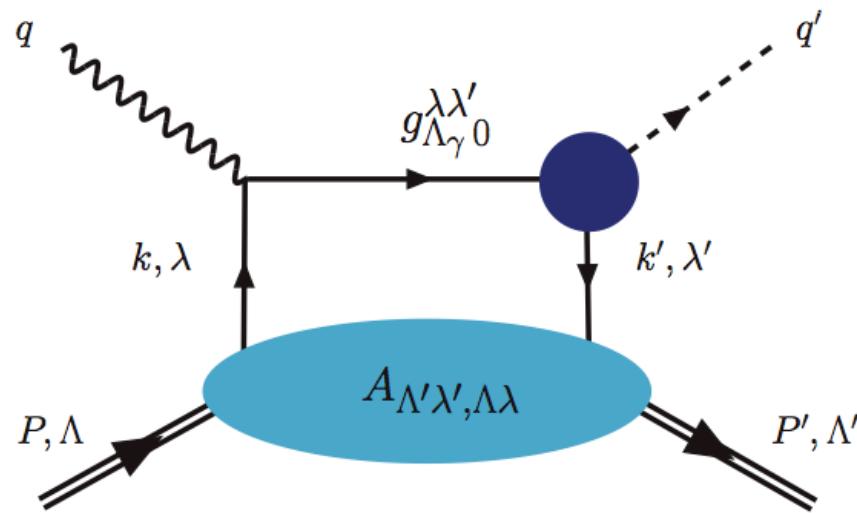
- ✓ Proof at twist two for longitudinal polarization given in J.C. Collins, L. Frankfurt, and M. Strikman, Phys. Rev. D 56, 2982 (1997).
- ✓ No proof at twist three exists as of yet
- ✓ A Q^2 “scan” at the EIC will be fundamental

2. CHIRAL ODD GPD'S

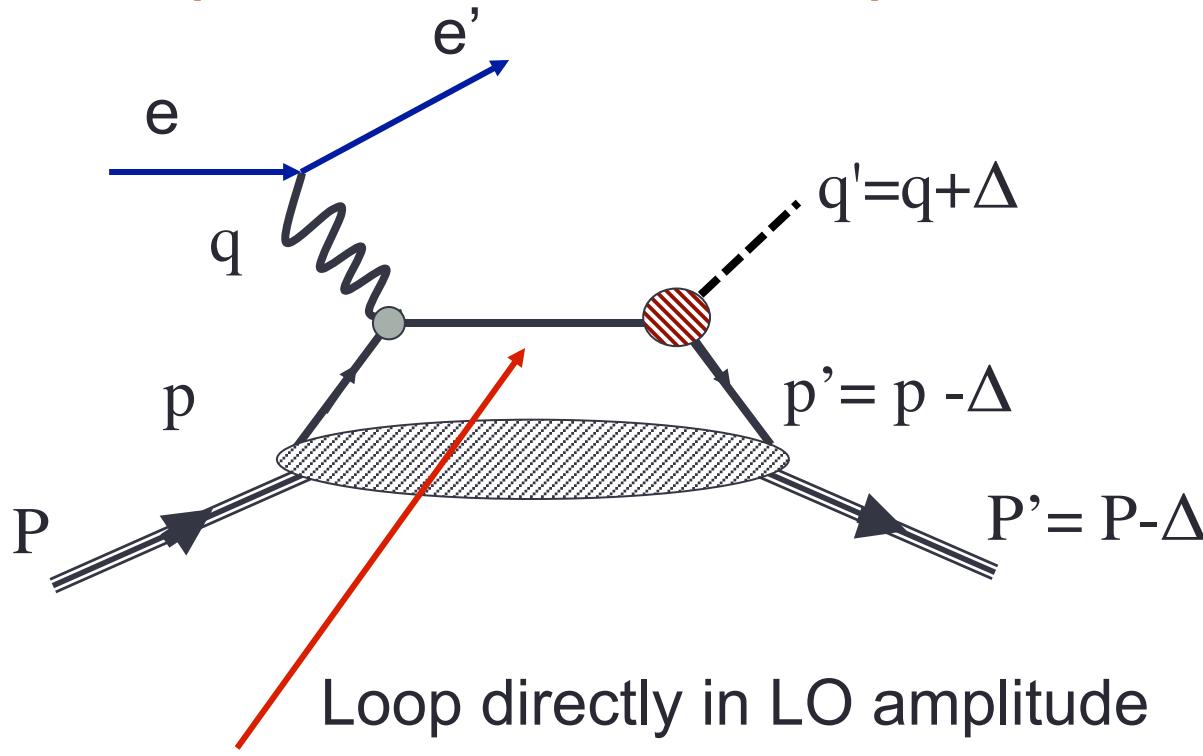
$$e p \rightarrow e' p' \pi^o$$

The non-local matrix elements probed are

$$\langle P' | \bar{u}(\xi) \sigma_{\mu\nu} u(0) | P \rangle$$



Deeply virtual pseudoscalar meson production

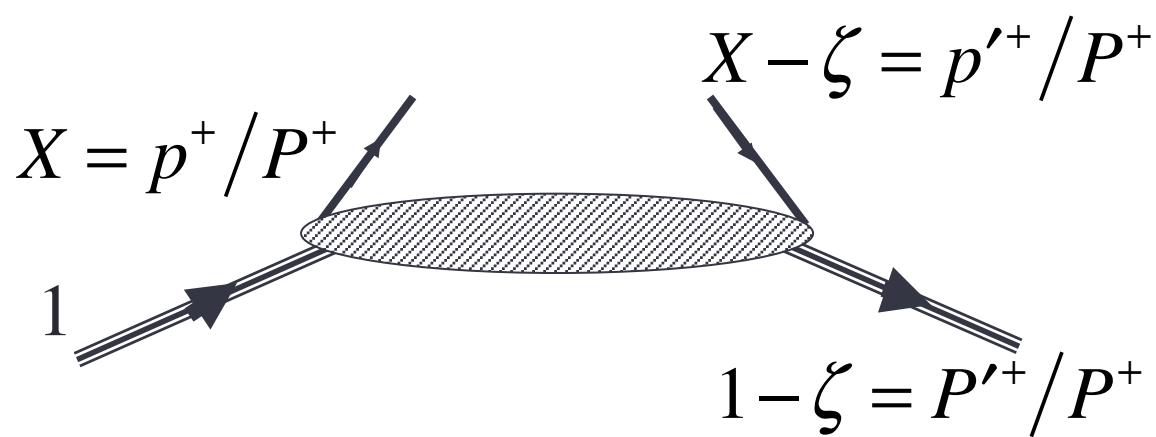
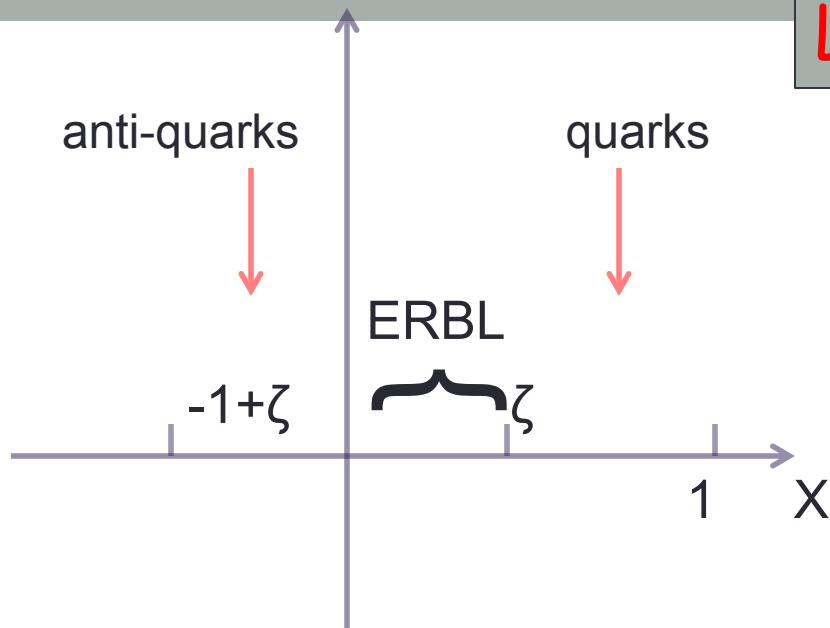


$$(1) \frac{1}{(p+q)^2 - m^2 + i\epsilon} = PV \frac{1}{(p+q)^2 - m^2} - i\pi \delta((p+q)^2 - m^2)$$

Both Re and Im parts are present

- (2) Quarks momenta and spins on LHS can be different from the RHS

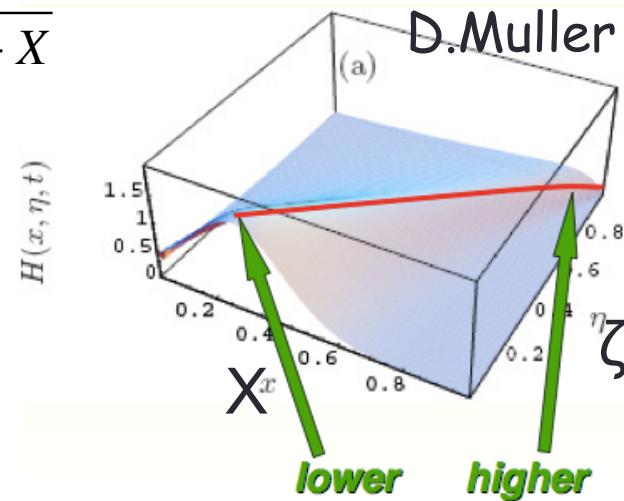
Light Cone Variables



Asymmetry in kinematics on LHS and RHS of diagram

$$\frac{1}{(p+q)^2 - m^2 + i\varepsilon} = PV \frac{1}{(p+q)^2 - m^2} - i\pi \delta((p+q)^2 - m^2)$$

$$\rightarrow \frac{1}{-Q^2 + 2(pq) + i\varepsilon} \rightarrow \frac{1}{-Q^2 / 2(Pq) + (pq) / (Pq)} = \frac{1}{-\zeta + X}$$



Amplitude

$$\mathcal{F}_q = P.V. \int_{-1+\zeta} dX F_q(X, \zeta, t) \left[\frac{1}{\zeta - X} - \frac{1}{X} \right] + i \pi e_q^2 F_q(\zeta, \zeta, t)$$

GPD

Compton Form Factor

GPD on “ridge”

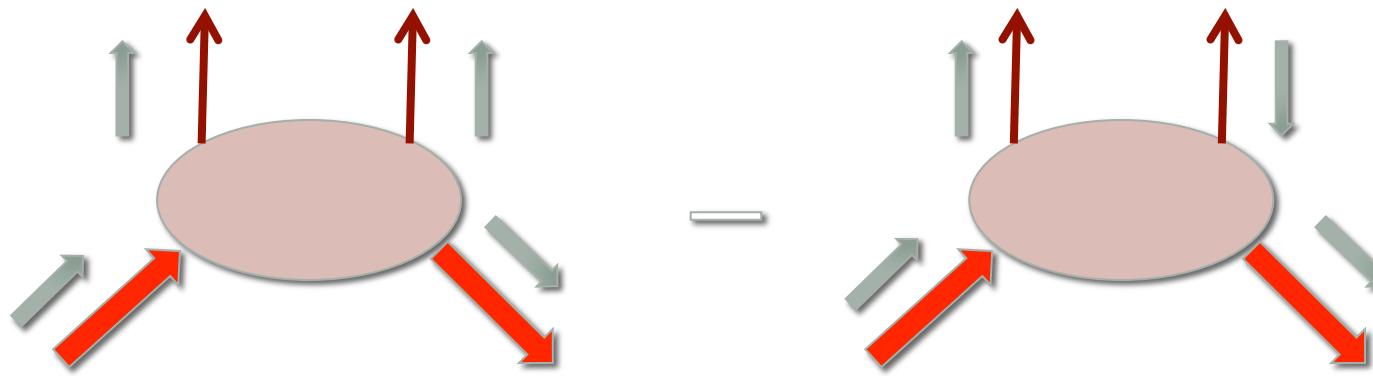
Quark correlator in the chiral odd sector

$$\begin{aligned} W_{\Lambda', \Lambda}^{[i\sigma^{i+}\gamma_5]}(x, \xi, t) = & \overline{U}(P', \Lambda') \left(i\sigma^{+i} H_T(x, \xi, t) + \frac{\gamma^+ \Delta^i - \Delta^+ \gamma^i}{2M} E_T(x, \xi, t) \right. \\ & \left. + \frac{P^+ \Delta^i - \Delta^+ P^i}{M^2} \tilde{H}_T(x, \xi, t) + \frac{\gamma^+ P^i - P^+ \gamma^i}{2M} \tilde{E}_T(x, \xi, t) \right) U(P, \Lambda) \end{aligned}$$

One to one relation with helicity amplitudes

$$\begin{aligned}
 A_{++,--} &= \frac{\sqrt{1-\zeta}}{1-\zeta/2} \left[H_T + \frac{t_0-t}{4M^2} \tilde{H}_T + \frac{\zeta^2/4}{1-\zeta} E_T + \frac{\zeta/2}{1-\zeta} \tilde{E}_T \right] \\
 A_{+-,-+} &= -\frac{\sqrt{1-\zeta}}{1-\zeta/2} \frac{t_0-t}{4M^2} \tilde{H}_T \\
 A_{++,-+} &= \frac{\sqrt{t_0-t}}{2M} \left[\tilde{H}_T + \frac{1-\zeta}{2-\zeta} E_T + \frac{1-\zeta}{2-\zeta} \tilde{E}_T \right], \\
 A_{-+,-+} &= \frac{\sqrt{t_0-t}}{2M} \left[\tilde{H}_T + \frac{1}{2-\zeta} E_T + \frac{1}{2-\zeta} \tilde{E}_T \right].
 \end{aligned}$$

Chiral Even Quark-Proton Helicity Amplitudes



$$A_{\Lambda'\pm,\Lambda\pm} \Leftrightarrow H, E, \tilde{H}, \tilde{E}$$

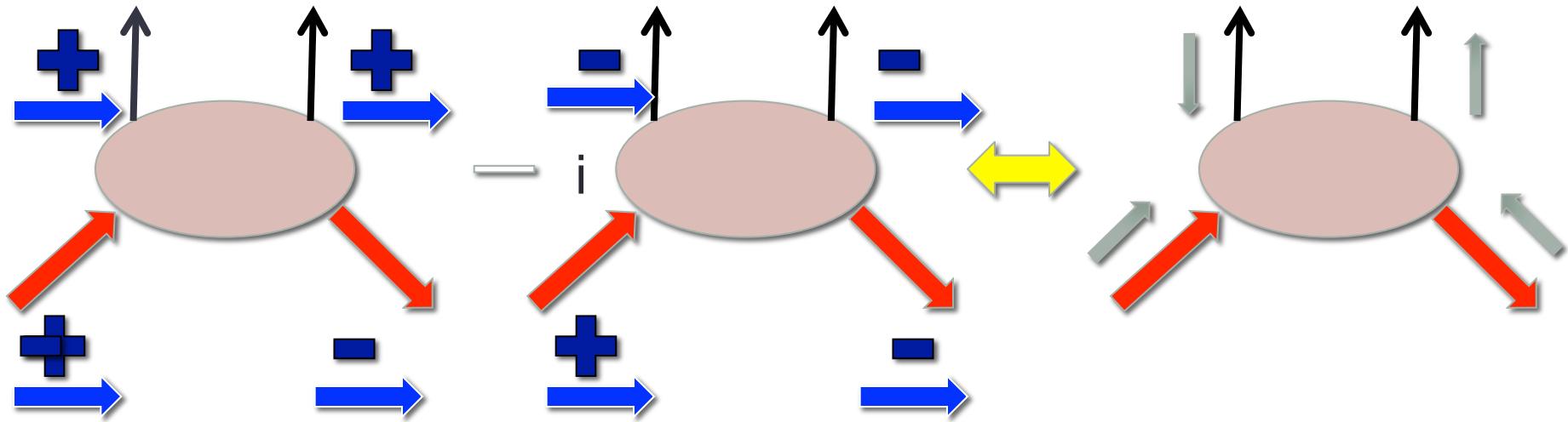
Net **helicity** of a quark in a **longitudinally polarized** proton:

$$g_1(x, Q^2) \Rightarrow \int_0^1 dx g_1(x, Q^2) = g_A$$

Chiral Odd Quark-Proton Helicity Amplitudes

$$|\uparrow\downarrow\rangle_Y = |\rightarrow\rangle \pm i |\leftarrow\rangle$$

$$A_{\Lambda'\pm,\Lambda\mp} \Leftrightarrow H_T, E_T, \tilde{H}_T, \tilde{E}_T$$

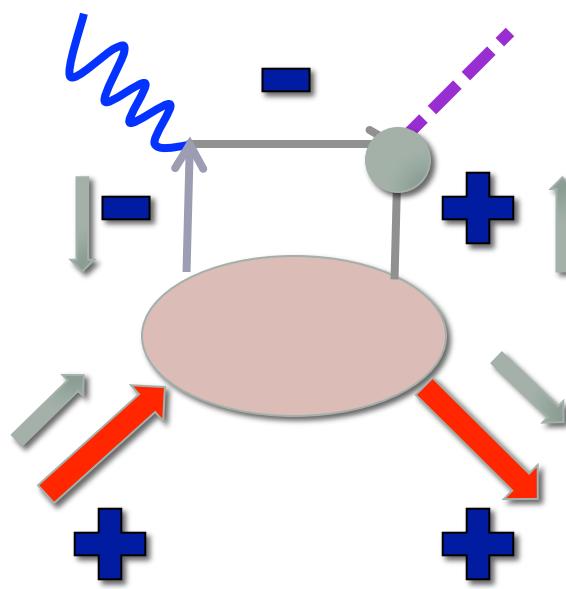


Net transverse polarization of a quark in a transversely polarized proton:

$$h_1(x, Q^2) \Rightarrow \int_0^1 dx h_1(x, Q^2) = \delta(Q^2)$$

In the helicity basis it is described in terms of non-diagonal/chirally-odd quark-proton helicity amplitudes.

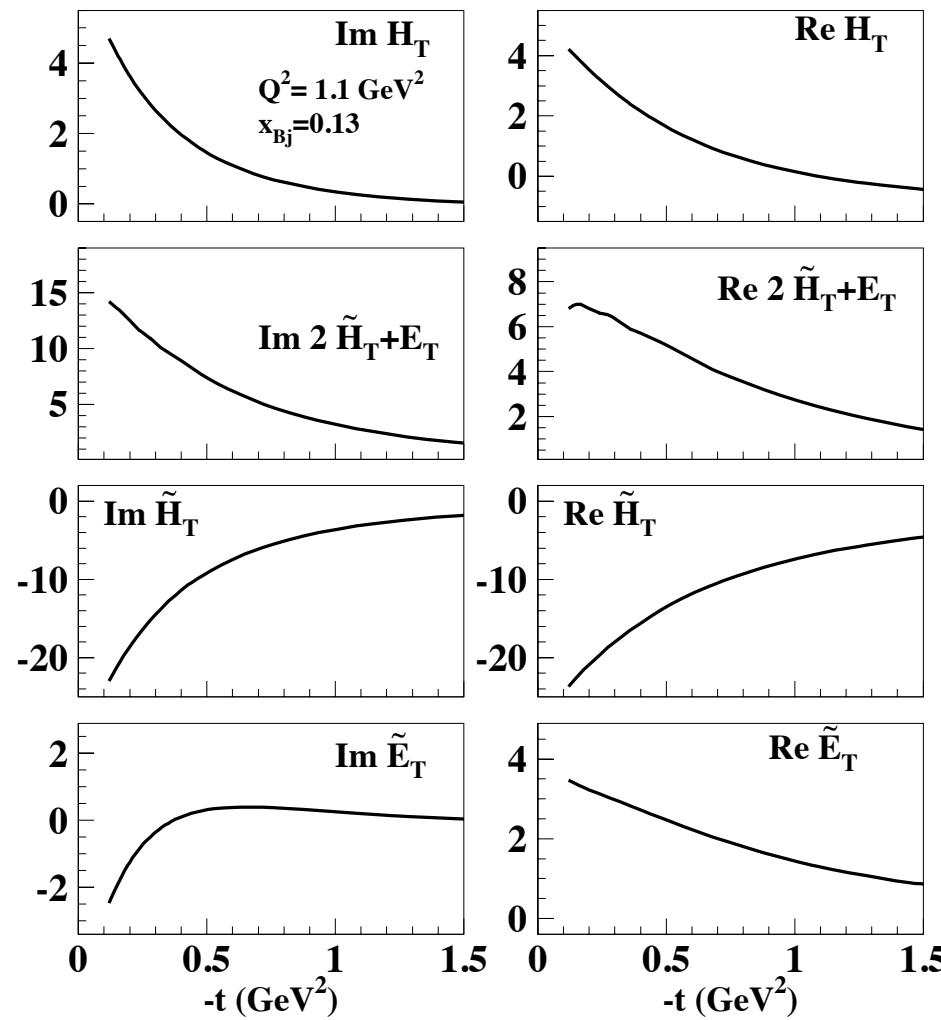
One can disentangle all four configurations, for example:



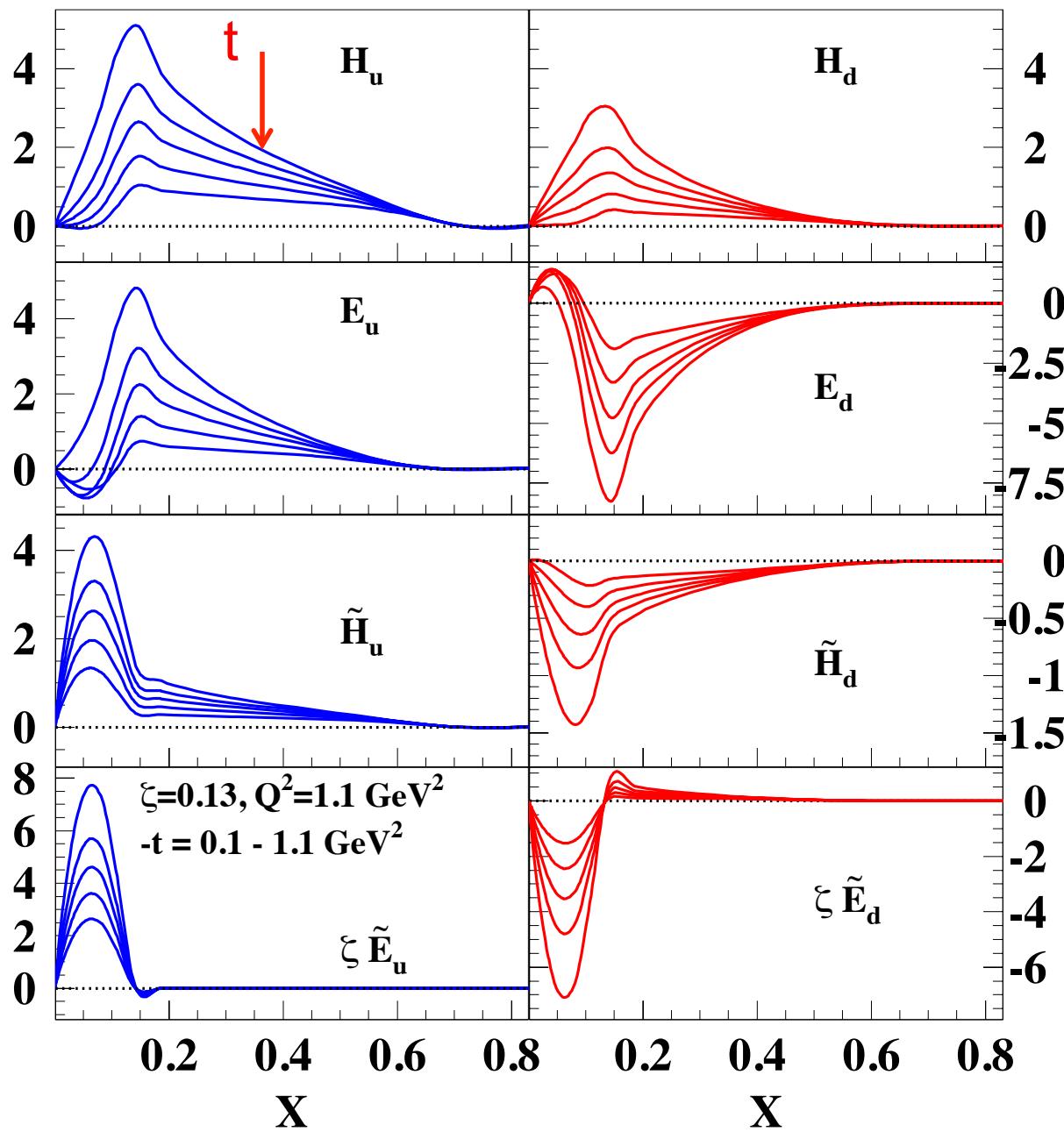
$$A_{+-,++}$$



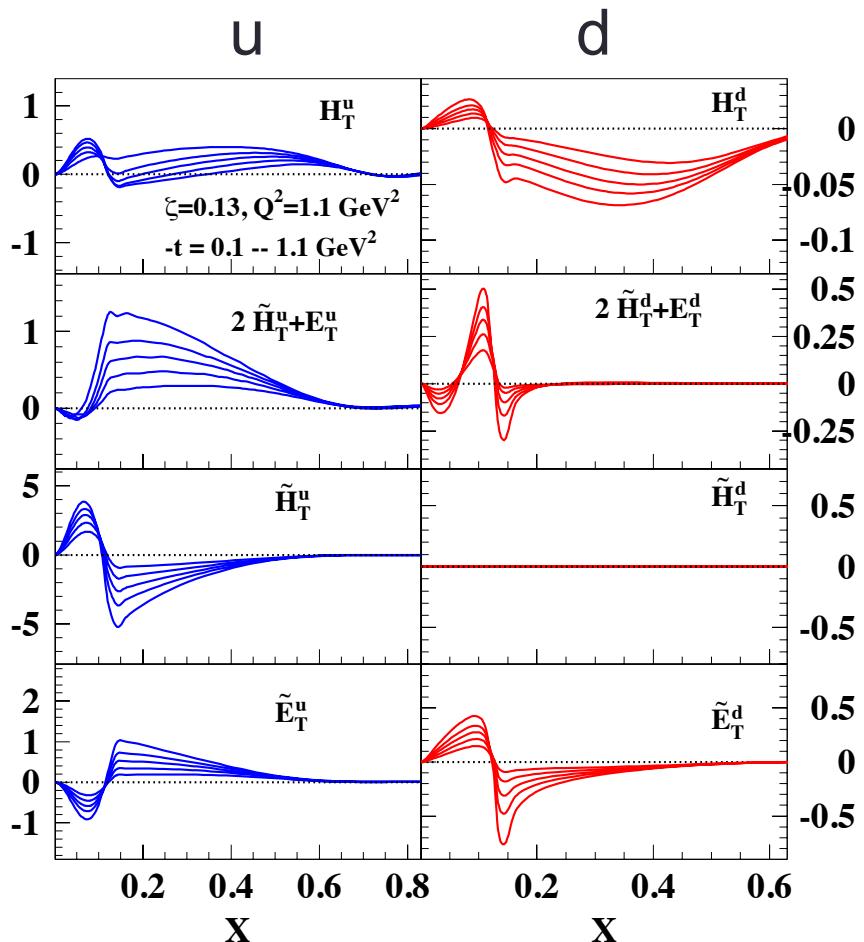
$$2\tilde{H}_T + E_T$$



Chiral even GPDs



The Chiral Odd sector is vastly unexplored



tensor charge

$$\int dx H_T^q(x, \zeta, t, Q^2) = \delta_q(t, Q^2)$$

tensor anomalous magnetic moment

$$\int dx [2\tilde{H}_T^q(x, \zeta, t, Q^2) + E_T^q(x, \zeta, t, Q^2)] = \kappa_q(t, Q^2)$$

(M. Burkardt, PRD66, 114005 (2002))



G. Goldstein, O. Gonzalez-Hernandez, S.L.,
PRD(2015) arXiv:1311.0483

Predictions based on the reggeized diquark model



The image shows a screenshot of the Physical Review D journal website. The header is teal-colored with white text. It reads "PHYSICAL REVIEW D" in large capital letters, followed by "covering particles, fields, gravitation, and cosmology" in a smaller, italicized font. Below the header is a navigation bar with links: "Highlights", "Recent", "Accepted", "Authors", "Referees", "Search", "Press", "About", and a feed icon. The main content area is white and features a large, bold title: "Flexible parametrization of generalized parton distributions: The chiral-odd sector". Below the title, the authors are listed as "Gary R. Goldstein, J. Osvaldo Gonzalez Hernandez, and Simonetta Liuti" and the publication details are given as "Phys. Rev. D **91**, 114013 – Published 8 June 2015".

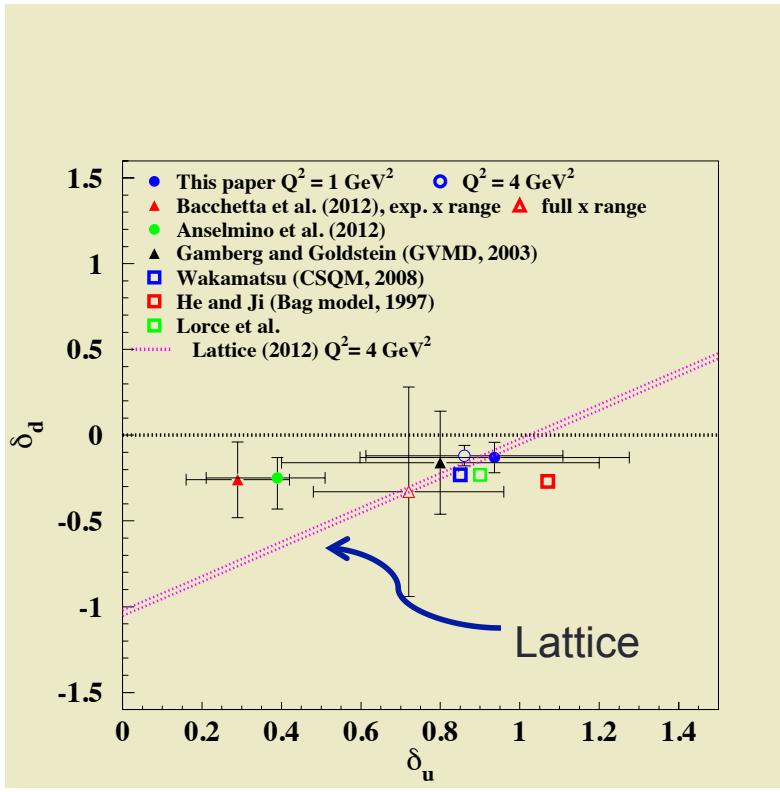
PHYSICAL REVIEW D
covering particles, fields, gravitation, and cosmology

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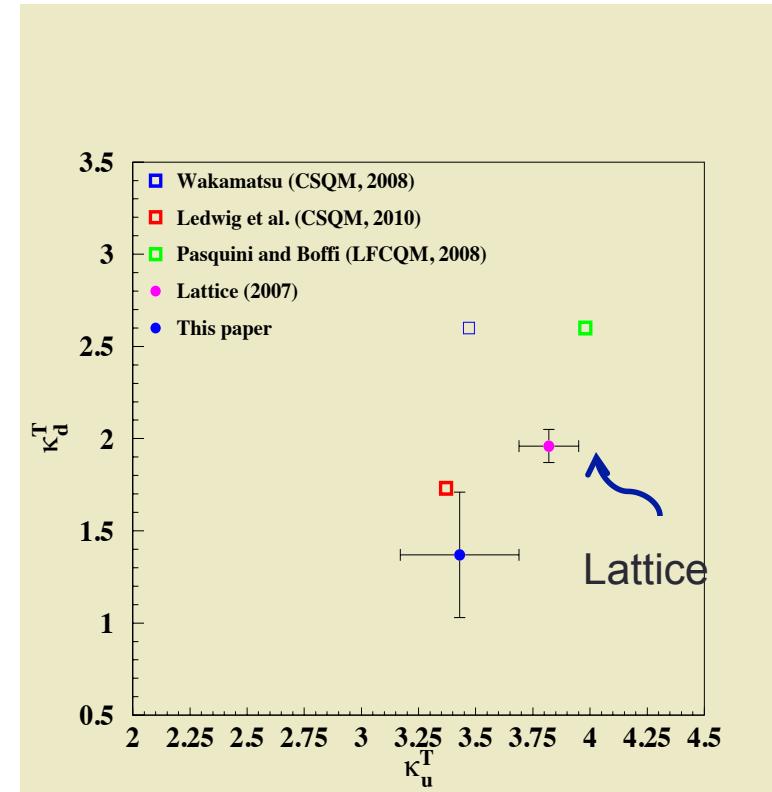
Flexible parametrization of generalized parton distributions: The chiral-odd sector

Gary R. Goldstein, J. Osvaldo Gonzalez Hernandez, and Simonetta Liuti
Phys. Rev. D **91**, 114013 – Published 8 June 2015

arXiv:1401.0438 [hep-ph]



J.~R.~Green, J.~W.~Negele, A.~V.~Pochinsky,
 S.~N.~Syritsyn, M.~Engelhardt and S.~Krieg,
 ``Nucleon Scalar and Tensor Charges from
 Lattice QCD with Light Wilson Quarks,"
Phys.\ Rev.\ D {\bf 86}, 114509 (2012)

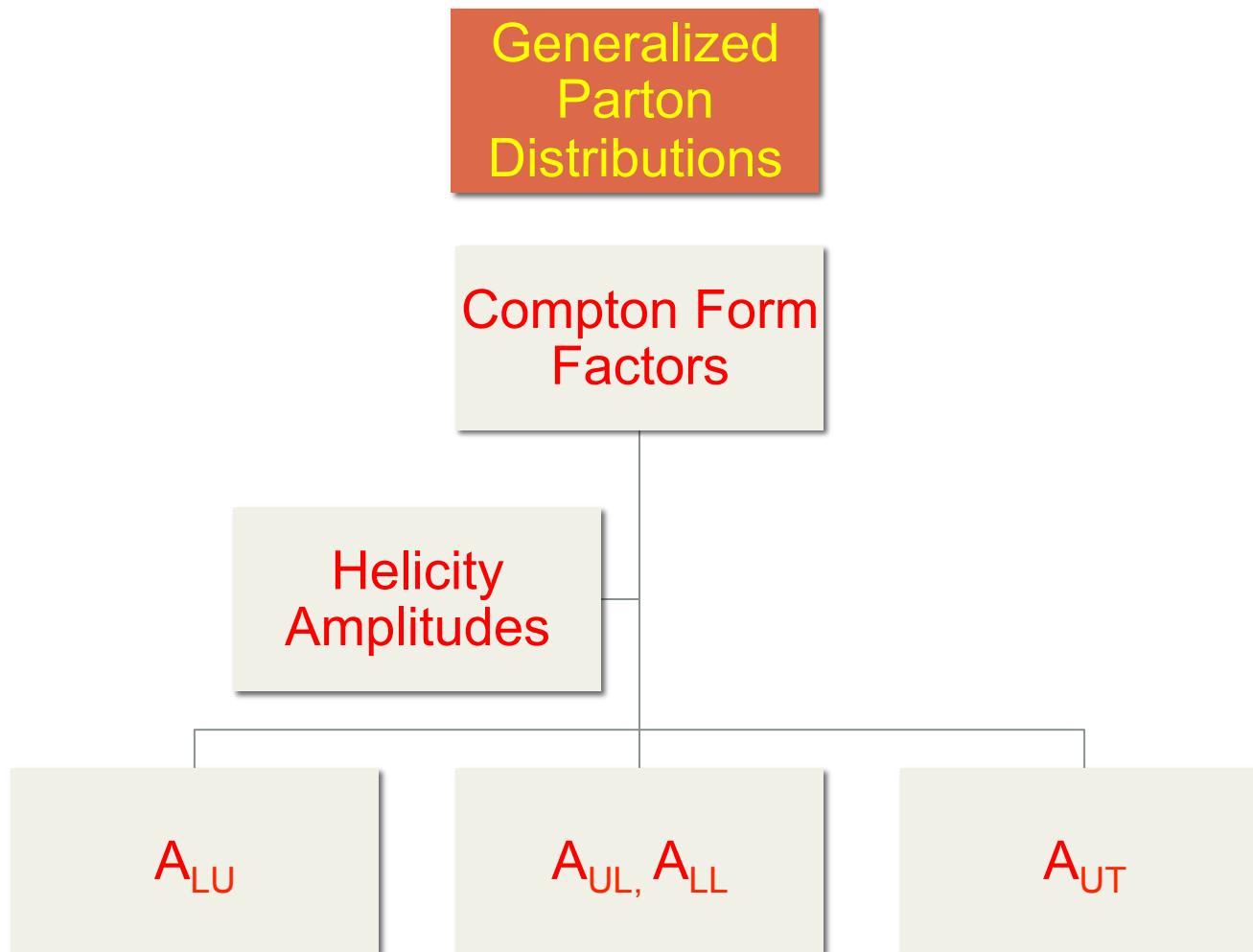


M. Gockeler et al. [QCDSF and UKQCD Collaborations], *Phys. Rev. Lett.* {\bf 98}, 222001 (2007)

3. EXTRACTION FROM EXPERIMENT

Experiment: DV π^0 P, DV η P

(Hall B, H. Avakian et al, Hall A. F. Sabatie et al)



Cross Section Formulation

Goldstein, Gonzalez Hernandez, S.L. Phys.Rev. D91 (2015)

$$\frac{d^4\sigma}{dx_B dy d\phi dt} = \Gamma \left\{ \begin{array}{l} F_{UU,T} + \epsilon F_{UU,L} + \epsilon \cos 2\phi F_{UU}^{\cos 2\phi} + \sqrt{2\epsilon(\epsilon+1)} \cos \phi F_{UU}^{\cos \phi} + h \sqrt{2\epsilon(1-\epsilon)} \sin \phi F_{LU}^{\sin \phi} \\ + S_{||} \left[\sqrt{2\epsilon(\epsilon+1)} \sin \phi F_{UL}^{\sin \phi} + \epsilon \sin 2\phi F_{UL}^{\sin 2\phi} + h \left(\sqrt{1-\epsilon^2} F_{LL} + \sqrt{2\epsilon(1-\epsilon)} \cos \phi F_{LL}^{\cos \phi} \right) \right] \\ + S_{\perp} \left[\sin(\phi - \phi_S) \left(F_{UT,T}^{\sin(\phi-\phi_S)} + \epsilon F_{UT,L}^{\sin(\phi-\phi_S)} \right) + \epsilon \left(\sin(\phi + \phi_S) F_{UT}^{\sin(\phi+\phi_S)} + \sin(3\phi - \phi_S) F_{UT}^{\sin(3\phi-\phi_S)} \right) \right. \\ + \sqrt{2\epsilon(1+\epsilon)} \left(\sin \phi_S F_{UT}^{\sin \phi_S} + \sin(2\phi - \phi_S) F_{UT}^{\sin(2\phi-\phi_S)} \right) \\ \left. + S_{\perp} h \left[\sqrt{1-\epsilon^2} \cos(\phi - \phi_S) F_{LT}^{\cos(\phi-\phi_S)} + \sqrt{2\epsilon(1-\epsilon)} \left(\cos \phi_S F_{LT}^{\cos \phi_S} + \cos(2\phi - \phi_S) F_{LT}^{\cos(2\phi-\phi_S)} \right) \right] \right\} \end{array} \right.$$

GPDs
in helicity
amplitudes



$$F_{UU,T} = \mathcal{N} [|f_{10}^{++}|^2 + |f_{10}^{+-}|^2 + |f_{10}^{-+}|^2 + |f_{10}^{--}|^2]$$

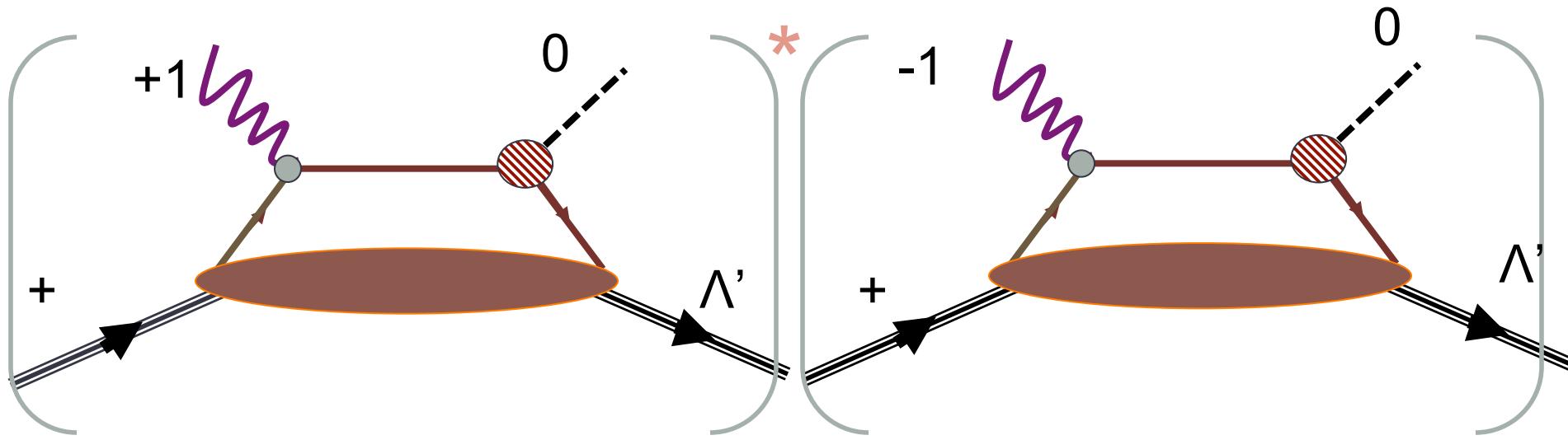
$$F_{UU,L} = \mathcal{N} [|f_{00}^{++}|^2 + |f_{00}^{+-}|^2]$$

$$F_{UU}^{\cos 2\phi} = -\mathcal{N} 2\Re e [(f_{10}^{++})^*(f_{10}^{--}) - (f_{10}^{+-})^*(f_{10}^{-+})]$$

$$F_{UU}^{\cos \phi} = -\mathcal{N} \Re e [(f_{00}^{+-})^*(f_{10}^{+-} + f_{10}^{-+}) + (f_{00}^{++})^*(f_{10}^{++} - f_{10}^{--})]$$

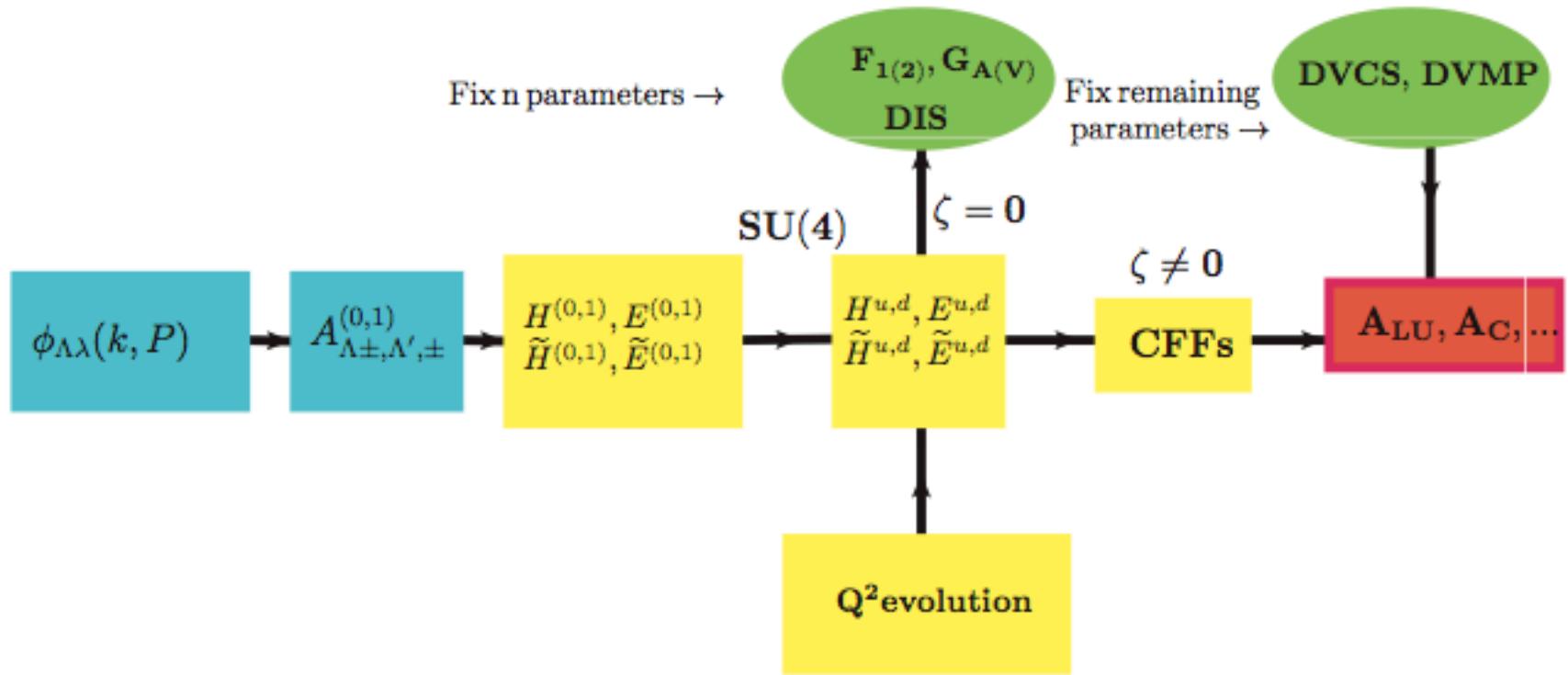
$$F_{LU}^{\sin \phi} = \mathcal{N} \Im m [(f_{00}^{+-})^*(f_{10}^{+-} + f_{10}^{-+}) + (f_{00}^{++})^*(f_{10}^{++} - f_{10}^{--})]$$

General form of structure function of a chiral odd term:

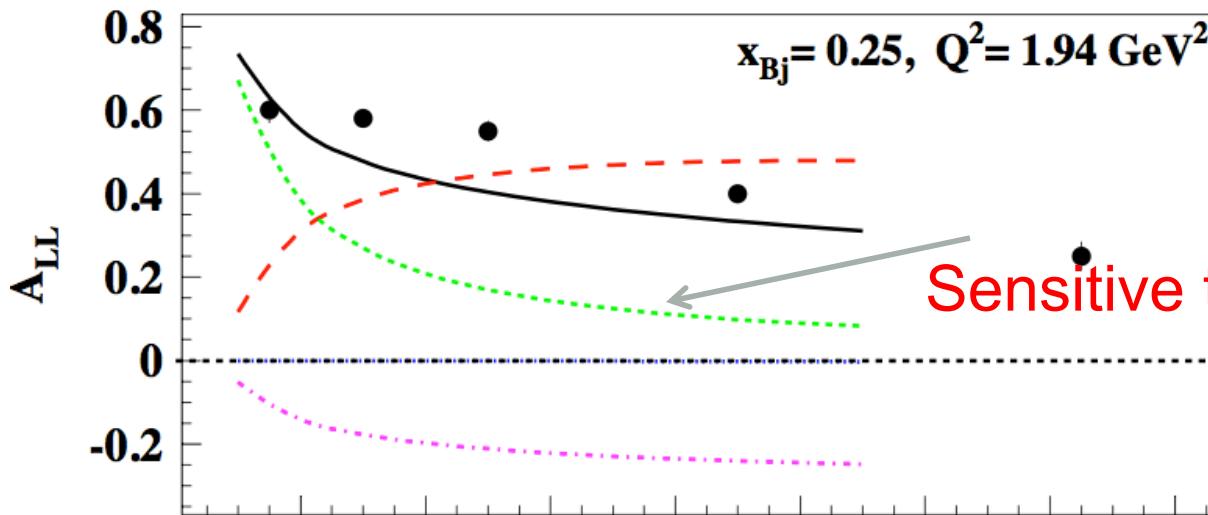


helicity amplitudes

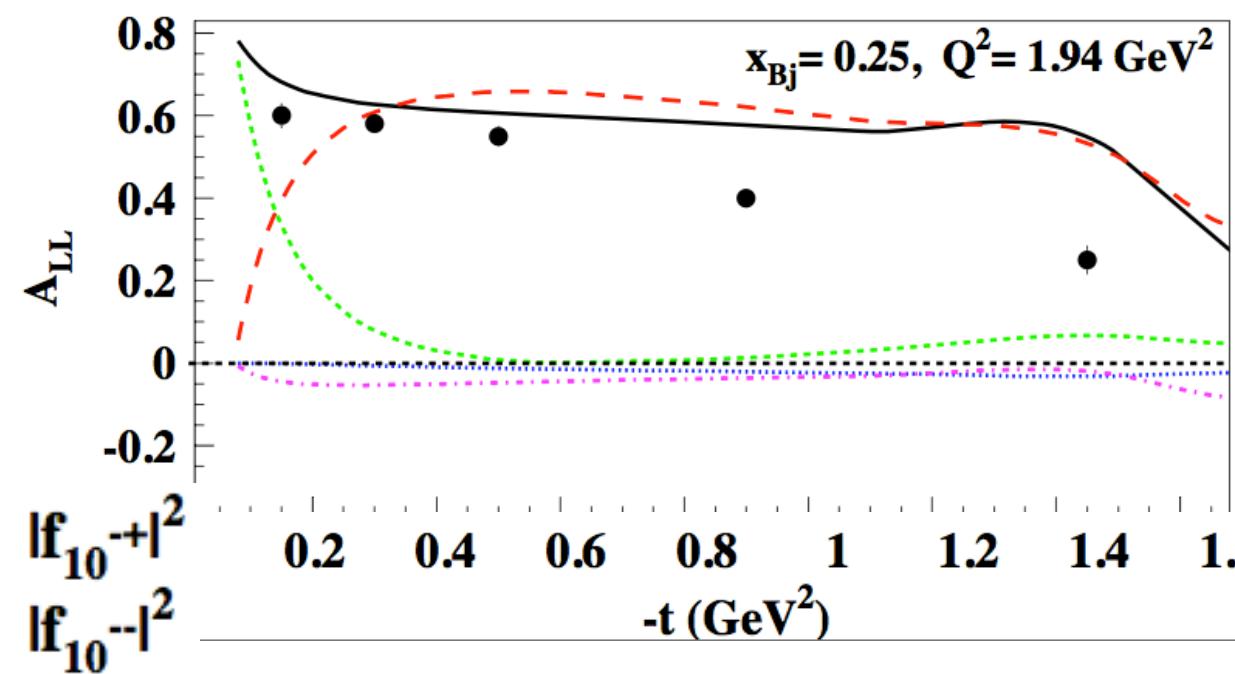
$$F_{1,-1}^{++} = \sum_{\Lambda'} \left(f_{10}^{+\Lambda'} \right)^* \left(f_{-10}^{+\Lambda'} \right)$$



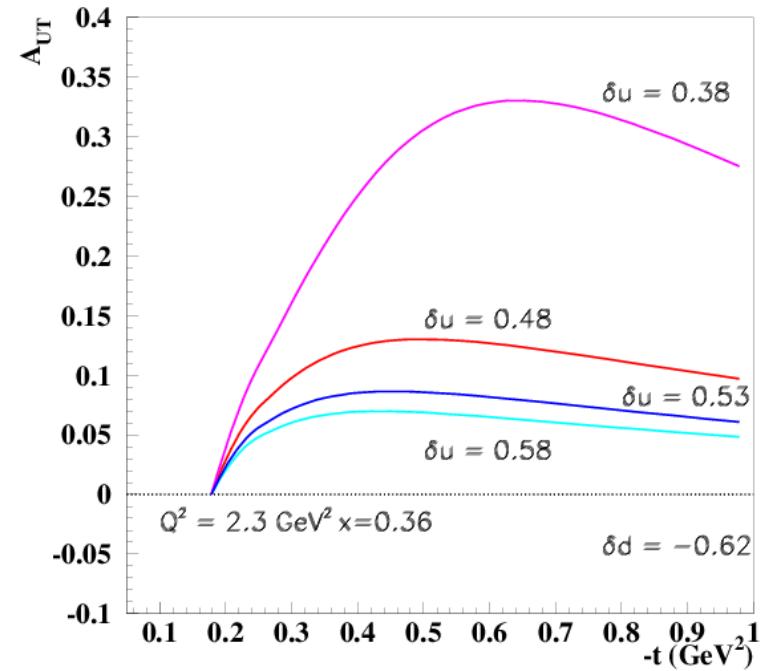
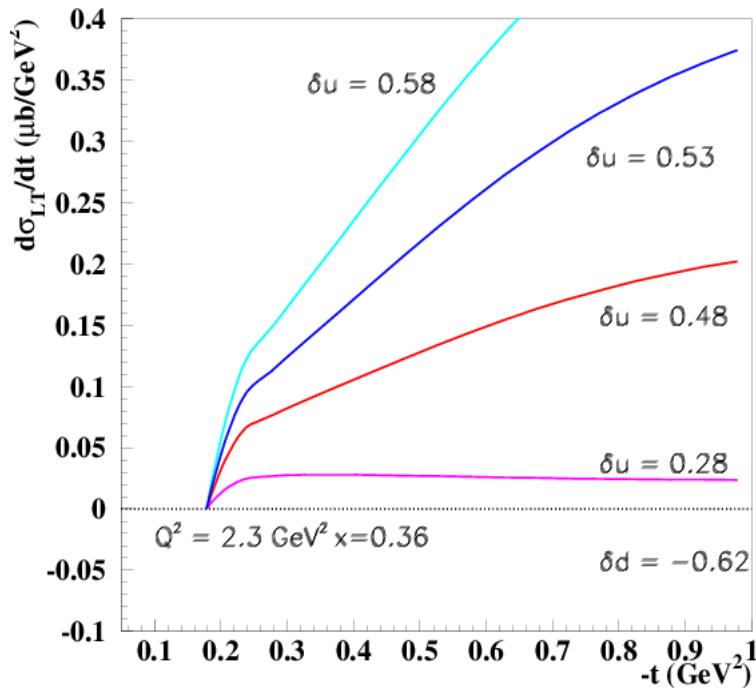
Andrey Kim, Harut Avakian et al., Jefferson Lab CLAS Collaboration



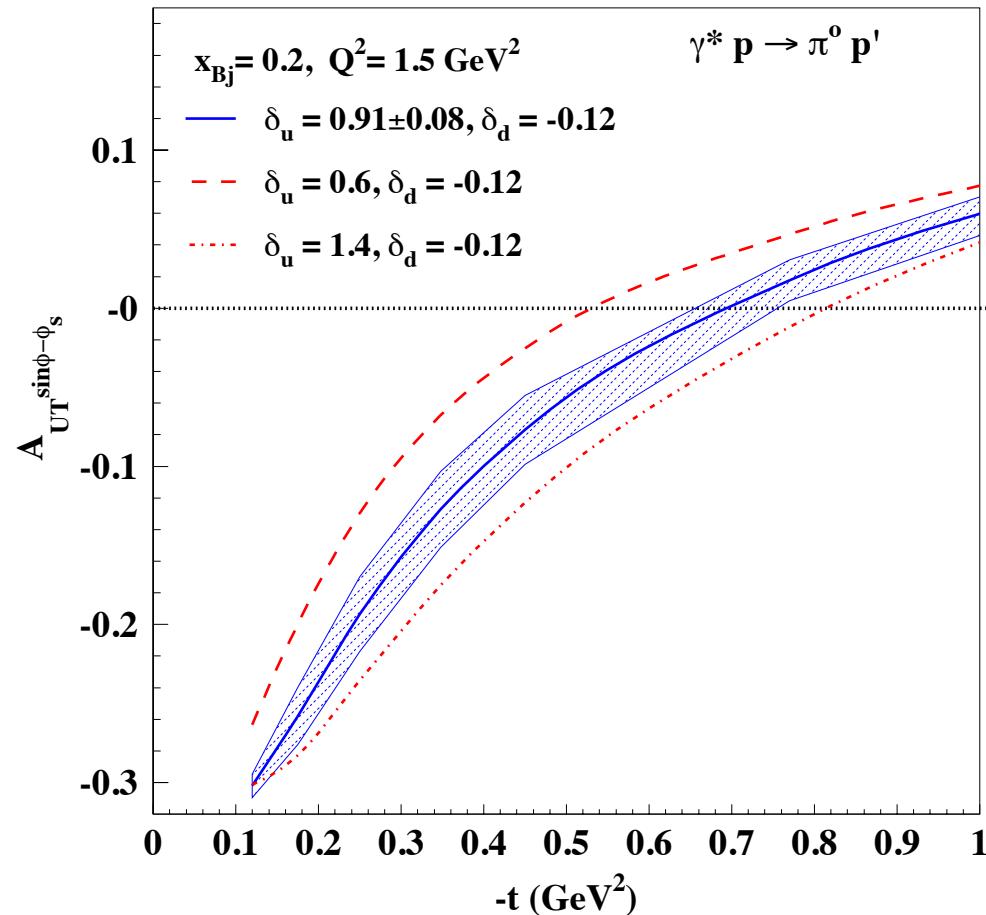
Role of parameters



Tensor Charge and Anomalous Transverse Moment treated as free parameters to be extracted from data



Projections for transverse polarized target



4. IMPACT ON BSM SEARCHES

Based on

PHYSICAL REVIEW LETTERS

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Beyond-Standard-Model Tensor Interaction and Hadron Phenomenology

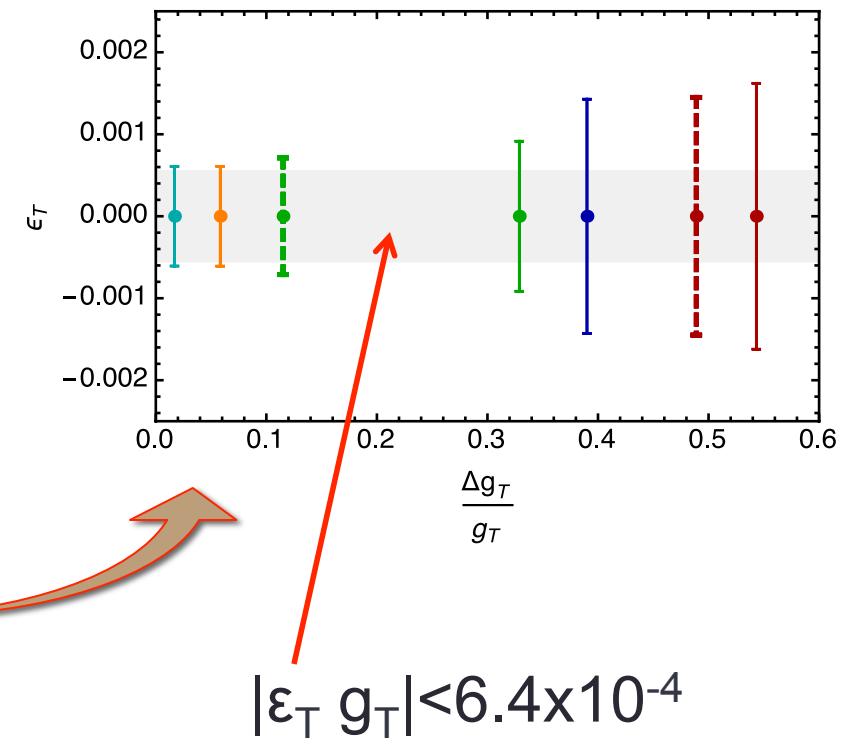
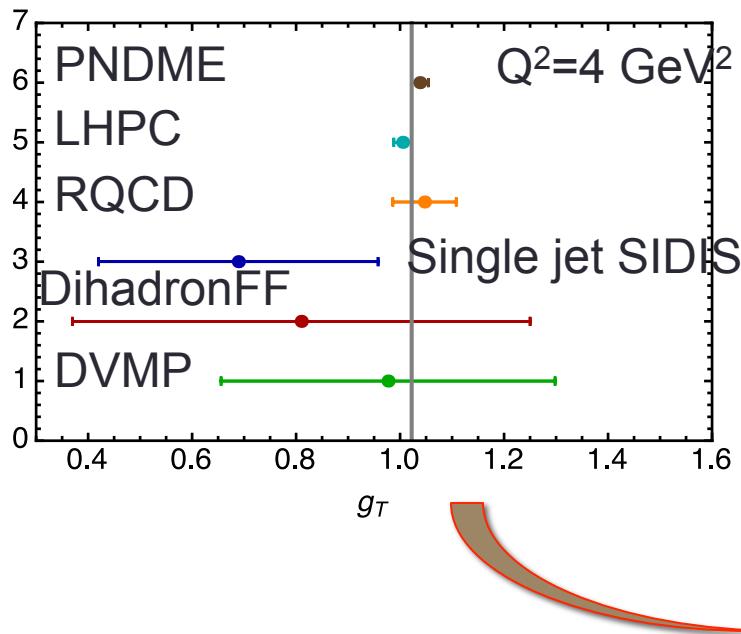
Aurore Courtoy, Stefan Baeßler, Martín González-Alonso, and Simonetta Liuti

Phys. Rev. Lett. **115**, 162001 – Published 15 October 2015

Why is the tensor charge interesting?

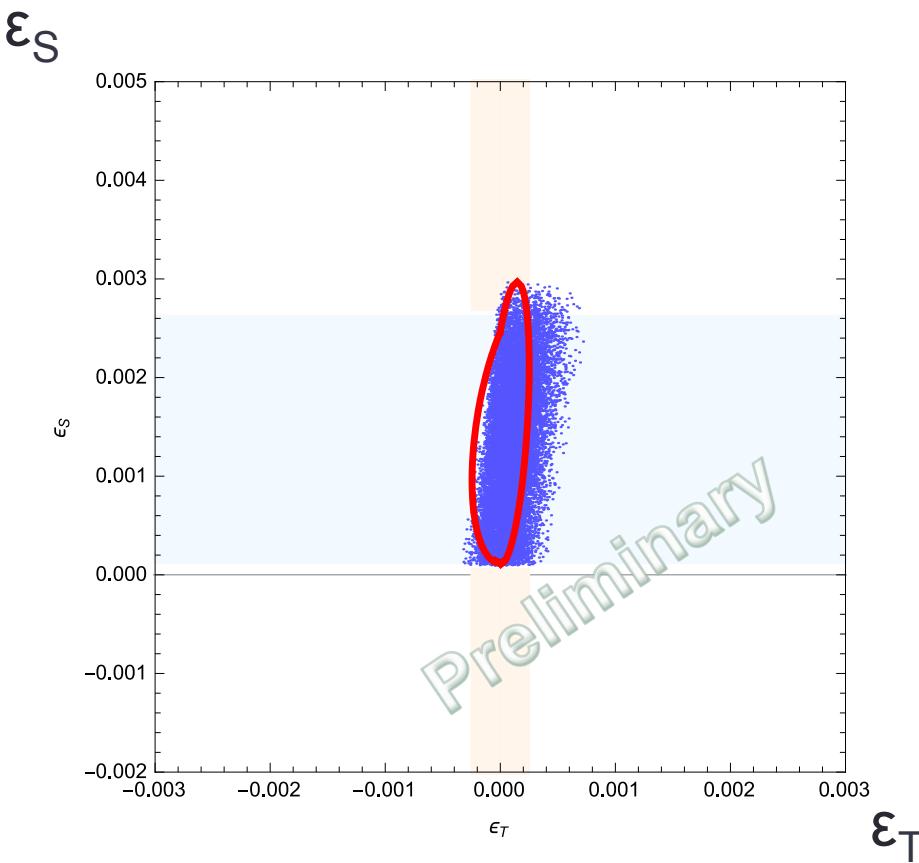
- ✓ It describes a specific response of the nucleon to polarization
but it is not a fundamental property → composite structure
- ✓ It evolves in PQCD but it does not couple to gluons (valence-like structure)
- ✓ Because the anomalous dimensions do not vanish for the first Mellin moment, the tensor charge evolves with Q^2

Impact on BSM searches...



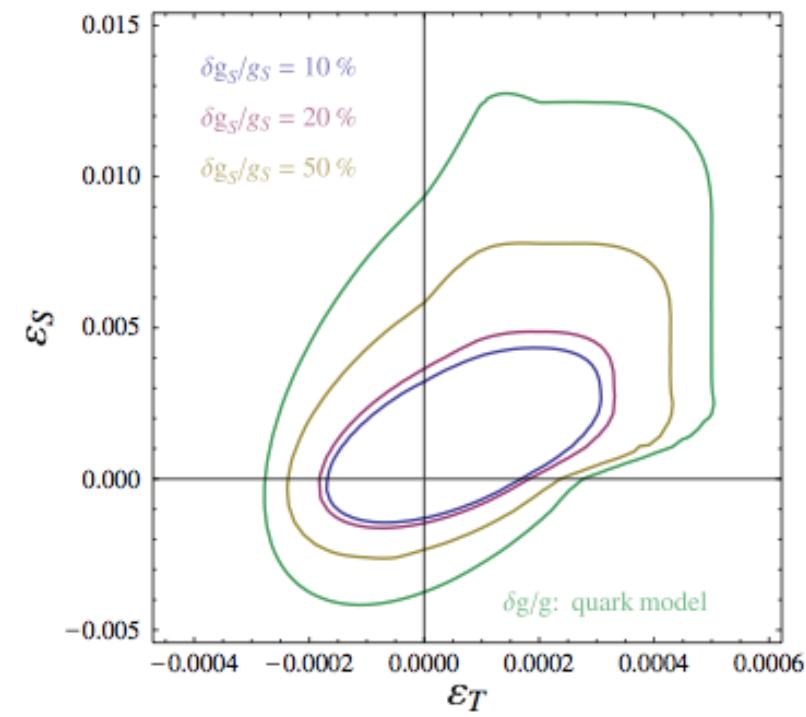
Pattie et al, PRC88 (2013)

New Analysis (Pavia, UNAM, NMSU, Virginia)



g_S from J. Martin-Camalich + M. Gonzalez-Alonso, PRL (2014)

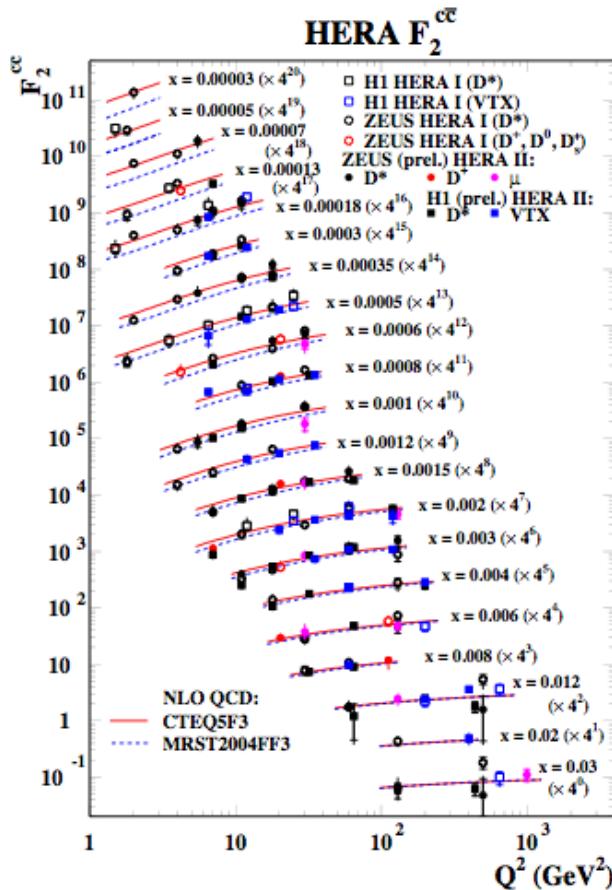
Combined 90% confidence level in ϵ_S - ϵ_T plane



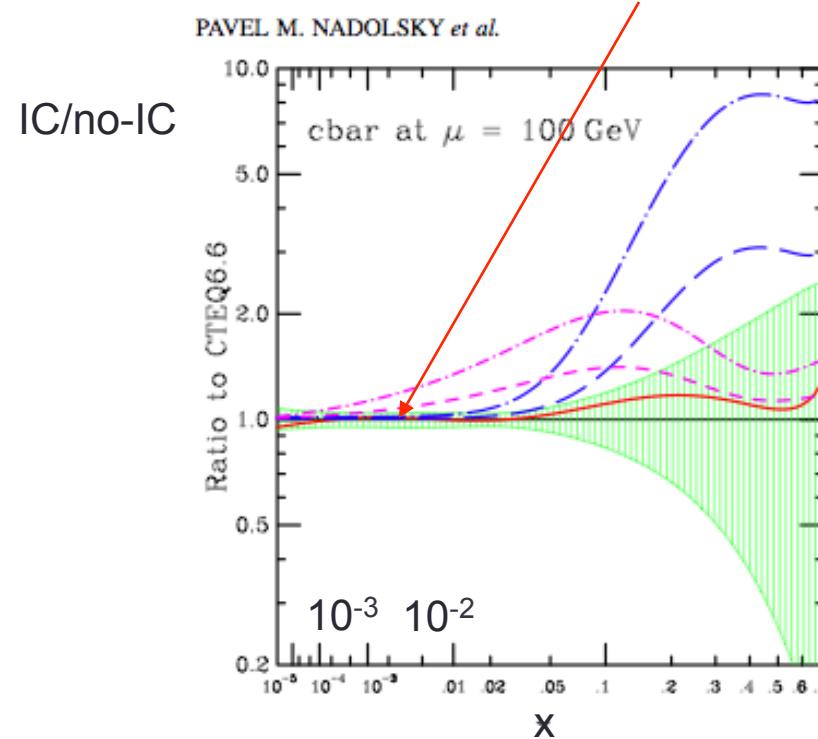
Lattice Extraction
Bhattacharya et al., PRD85 (2012)

5. FUTURE DEVELOPMENTS

5.1 Deeply Virtual Exclusive Processes with Charm



Data are at very low x where they cannot discriminate whether Intrinsic Charm is there



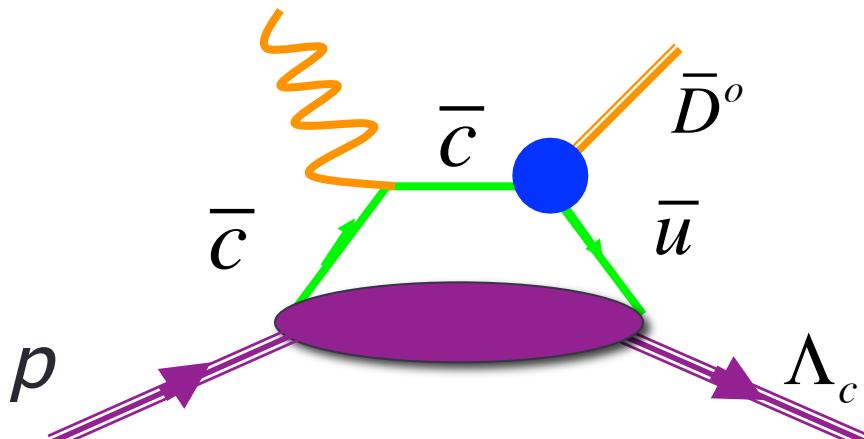
A window into heavy flavor production at the EIC

$$\gamma^* p \rightarrow \eta_c p'$$

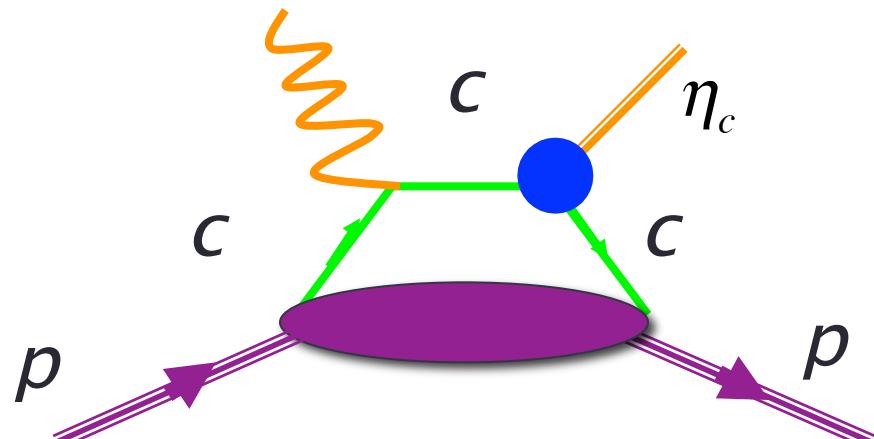
η_c , D^0 , and \bar{D}^0 exclusive production is governed by chiral-odd soft matrix elements (GPDs) which cannot evolve from gluons!

η_c , D^0 , and \bar{D}^0 used as triggers of “intrinsic charm content”!

(1)



(2)



$$p \rightarrow c\bar{c}uud \rightarrow (\bar{c}u)cud$$

$$p \rightarrow c\bar{c}uud \rightarrow (\bar{c}c)uud$$

5.2 A program to study BSM physivs

$$\langle p(p') | \bar{u} \sigma_{\mu\nu} d | n(p) \rangle \equiv \bar{u}_p(p') [g_T(q^2) \sigma^{\mu\nu} + g_T^{(1)}(q^2) (q^\mu \gamma^\nu - q^\nu \gamma^\mu) + g_T^{(2)}(q^2) (q^\mu P^\nu - q^\nu P^\mu) + g_T^{(3)}(q^2) (\gamma^\mu \not{q} \gamma^\nu - \gamma^\nu \not{q} \gamma^\mu)] u_n(p),$$

Study the additional currents

- Potential impact in axial vector sector studied by S. Gardner and B. Plaster, PRC87(2013)
- Connection with new chiral-odd GPDs
- Impact on EDM measurements
- More...

Conclusions and outlook

A vast program ahead of us that can be explored only with an EIC

A global analysis will allow us to extract the tensor charge from measurements of hard electron proton scattering processes (DVMP, Dihadron electroproduction, single jet SIDIS). This program can be developed at the EIC!!!!

The possibility of obtaining the scalar and tensor form factors and charges directly from experiment with sufficient precision, gives an entirely different leverage to neutron beta decay searches

The error on ϵ_T , depends on both the central value of g_T as well as on the relative error, $\Delta g_T / g_T$, therefore, independently from the theoretical accuracy that can be achieved, experimental measurements are essential since they simultaneously provide a testing ground for lattice QCD calculations.

A unique probe of intrinsic charm